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Experimental Observations on the Influence of Hydrogen Atoms Diffusion on Laminar and Turbulent Premixed Burning Velocities

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Abstract

Measurements of the laminar and turbulent burning velocity of premixed hydrogen – air, n-hexane – air and n-octane – air flames were made and compared to corresponding measurements of deuterium – air, n-hexane-d14 – air and n-octane-d18 – air flames performed at identical initial conditions. Experiments were conducted in a constant volume, optically accessed vessel, at elevated initial pressure and temperature of 0.5 MPa and 360 K, for a range of equivalence ratios. Burn rate data was determined via schlieren imaging of flames. It was found that the isotope effect accounted for an average reduction of 20% in the laminar burn rate of alkanes. Similarly, deuterium was measured to burn around 30% slower than hydrogen at the range of equivalence ratios explored. The isotope effect on burn rate was significantly reduced under turbulence. The difference between the turbulent burn rates of the deuterated alkanes and their normal alkane counterparts were measured to be approximately 10%. The difference between the turbulent burn rates of deuterium and hydrogen was even smaller. Nonetheless, the laminar burn rate ranking was maintained under turbulence for all fuels and conditions explored, thus suggesting a degree of influence of radical transport and chemistry under turbulent burning.

Keywords: laminar flames, turbulent flames, burning velocity, hydrogen combustion, deuterium combustion, isotope effect

Nomenclature

Latin Symbols

D	m^2/s	Mass diffusivity
k	$\text{m}^3/\text{mol.s}$	Reaction rate coefficient

44	L	m	Integral length scale of turbulence
45	L_b	m	Burnt Markstein length
46	P_i	Pa	Initial pressure
47	r_u	m	Cold flame mean flame radius
48	T_{ad}	K	Adiabatic flame temperature
49	T_i	K	Initial temperature
50	S	-	Laminar burning velocity sensitivity factor
51	u'	m/s	Turbulent root-mean-square velocity
52	u_l	m/s	Unstretched, one-dimensional laminar burning velocity
53	u_n	m/s	Stretched, entrainment laminar burning velocity
54	u_{te}	m/s	Entrainment turbulent burning velocity

55

56 Greek Symbols

57	α	m^2/s	Thermal diffusivity
58	α_{mix}	m^2/s	Thermal diffusivity of mixture
59	α	1/s	Flame stretch rate
60	δ_l	m	Laminar flame thickness
61	η	m	Kolmogorov length scale of turbulence
62	ϕ	-	Equivalence ratio
63	ω	$(m^3/mol.s)^n$	Global reaction rate

64

1. Introduction

The molecular structure of a fuel (i.e. length of chain, branching, bonding) is known to greatly influence the laminar burn rate [1-5]. Fuel structure in conjunction with mixture stoichiometry, pressure and temperature, govern the thermodynamics and chemical kinetics of combustion. One of the main driving forces of chemical kinetic contributions to the control of burning velocity is the radical pool at the flame front, with H atoms being the most important by virtue of their extremely high diffusivity and reactivity [4-5].

In two previous papers we investigated the effects of fuel structure on the laminar and turbulent burning velocities of gasoline components. We assessed:

- (i) isomeric structure and bonding through experimental studies of seven different hydrocarbons containing six carbon atoms, over a wide range of fuel - air mixtures [6] and
- (ii) chain length and molecular mass by reference to straight chain alkanes in the range $C_5 - C_8$ [7].

Interpretation of the results was linked to the influence of H radicals at the flame front in controlling the burn rate.

The object of the present work was to understand the importance of the transport and kinetic effects of hydrogen radicals within laminar and turbulent premixed flames via experimental studies of burning velocity measurements of freely propagating flames. Hence, we have extended the earlier studies [6, 7] through comparisons of laminar and turbulent velocity of n-hexane and n-octane (i.e. $n-C_6H_{14}$ and $n-C_8H_{18}$) with those of their fully deuterated forms (i.e. $n-C_6D_{14}$ and $n-C_8D_{18}$). In interpretation of the results, it is assumed that there are no qualitative differences in the kinetic mechanisms involved in flame propagation of the normal and deuterated fuels. In

addition, we explore the H / D isotopic effect in its most influential guise, via an investigation of the laminar and turbulent burning velocities of H₂ and D₂.

The available literature on the isotopomeric effects in combustion is sparse. With the exception of a study of laminar flame propagation in acetylene and di-deuteroacetylene by Friedman and Burke [8], we are not aware of any other investigation of the laminar and turbulent burn rates of deuterated versus normal hydrocarbons, even though the former are occasionally used for tracing the origins of pollutants in flames, e.g. [9]. Moreover, although hydrogen burn rate data exist for a variety of conditions [e.g. 10-18] there is only very little information on the laminar burn rates of D₂ [19-21] and, to our knowledge, no comparisons between the turbulent burn rates of H₂-air and D₂-air flames.

2. Experimental Apparatus and Data Processing

All measurements were performed in the Leeds MkII spherical bomb [22]. As in the previous studies for the examination of fuel structure and chain length effects on burn rate [6-7], measurements were performed at elevated temperature and pressure (360 K and 0.5 MPa), at which the premixed turbulent flames demonstrate behaviour similar to flames in spark-ignition engines [22]. Owing to the high cost of the deuterated fuels, the alkane tests were undertaken at only $\phi = 0.8$ and $\phi = 1.0$ for laminar conditions and at $\phi = 1.0$ under turbulent conditions. For the latter, the turbulence level was set at an rms velocity of $u' = 4$ m/s. The burn rates of H₂ and D₂ were examined for laminar and turbulent ($u' = 4$ m/s) conditions for $0.6 \leq \phi \leq 1.1$. The turbulence rms velocity of $u' = 4$ m/s chosen for this study was relevant to reciprocating engines, where u' near the top dead centre is about half the piston speed (e.g. $u' = 5$ m/s, for 75 mm stroke, at 4000 rpm [23]).

110 Premixed mixtures were prepared inside the fan-stirred vessel. Pre-calculated volumes of liquid
111 fuels were injected into the vessel under vacuum conditions, using a gas tight syringe. For
112 gaseous fuels, the mixture stoichiometry was controlled by measuring the partial pressure of the
113 fuel injected into the bomb at atmospheric pressure. The bomb fans were continuously operated
114 during mixture preparation to ensure full mixing and to assist heat transfer from the 2 kW
115 electrical heater, positioned close to the walls of the vessel. For laminar studies, the fans were
116 switched off for a period of 60 seconds, following mixture preparation, and before ignition. For
117 turbulent studies the fans were maintained at the speed required to produce the desired rms
118 turbulent velocity throughout the mixture preparation, ignition and combustion period. The
119 pressure in the vessel before ignition was measured via an absolute pressure transducer (Druck
120 PDCR-911) with a range of 0 to 0.7 MPa. Following spark discharge, the pressure rise in the
121 vessel was monitored with a Kistler-701 piezoelectric pressure transducer, flush mounted on the
122 side of the vessel. After each experiment the vessel was flushed several times with compressed
123 air and then evacuated. Dry cylinder air was provided for the combustible mixture.

124 At least two laminar and five turbulent deflagrations were performed at each condition. Centrally
125 ignited advancing flames were imaged via the schlieren method to the bomb window diameter of
126 150 mm, using a Photsonics Phantom Series 9 high speed digital camera. Laminar flames were
127 recorded at 4000 frames/s with a resolution of 576x576 pixels. Turbulent flames were
128 photographed at a rate of 9000 frames/s with a resolution of 384x384 pixels.

129 During post-processing of schlieren data, each flame image was converted from grayscale to
130 black and white. White corresponded to the burned and black to the unburned region. The flame
131 area was found by counting the number of white pixels. The burning velocity was then defined as
132 the radius derivative with respect to time divided by the ratio of densities of the fresh mixture to

that of the combustion products. Mean flame radius was determined as that of a circle encompassing the same area. Further information on the flame image processing procedure is given in [6, 24]. Imaging data analysis to obtain laminar flame characteristics (burning velocity, stretch rate and Markstein lengths) and turbulent burn rates followed established methods, detailed [25-26] and widely used elsewhere [eg. 27-31].

3. Results

Presented in this section are measured laminar and turbulent burn rate results for normal and deuterated alkanes, hydrogen and deuterium. Experimental scatter for laminar deflagrations was at a maximum of 2% with respect to the coefficient of variance (COV) of the laminar burning velocity at any given flame radius. Turbulent deflagrations reported here exhibited an average scatter of circa 7-8% in COV of the turbulent burn rate at a given flame radius, which was similar to that reported in [32] and is typical of the magnitude of cycle-to-cycle variation of the burning rate in an SI engine [33].

In addition to data for the unstretched, one dimensional, laminar burning velocity, u_l , derived in accord with [26], the laminar results for the alkanes also include data for the stretched laminar burning velocities, u_n , at mean flame radii of 10 mm and 30 mm. Due to the comparable molar mass of n-hexane versus n-hexane-d14 and n-octane versus n-octane-d18, stretch rate effects were anticipated to be similar and, therefore, to not affect the trends observed for the laminar burn rate ratio of normal vs deuterated alkanes.

For H_2 and D_2 laminar deflagrations, hydrodynamic flame instabilities [34-35] occurred too early to apply the criteria for unstretched laminar burning velocity [26]. It was thus decided to present

the schlieren-derived stretched burning velocities at mean flame radii of 10 mm and 30 mm to allow comparison to previous studies [13] and ensure exclusion of spark effects [36].

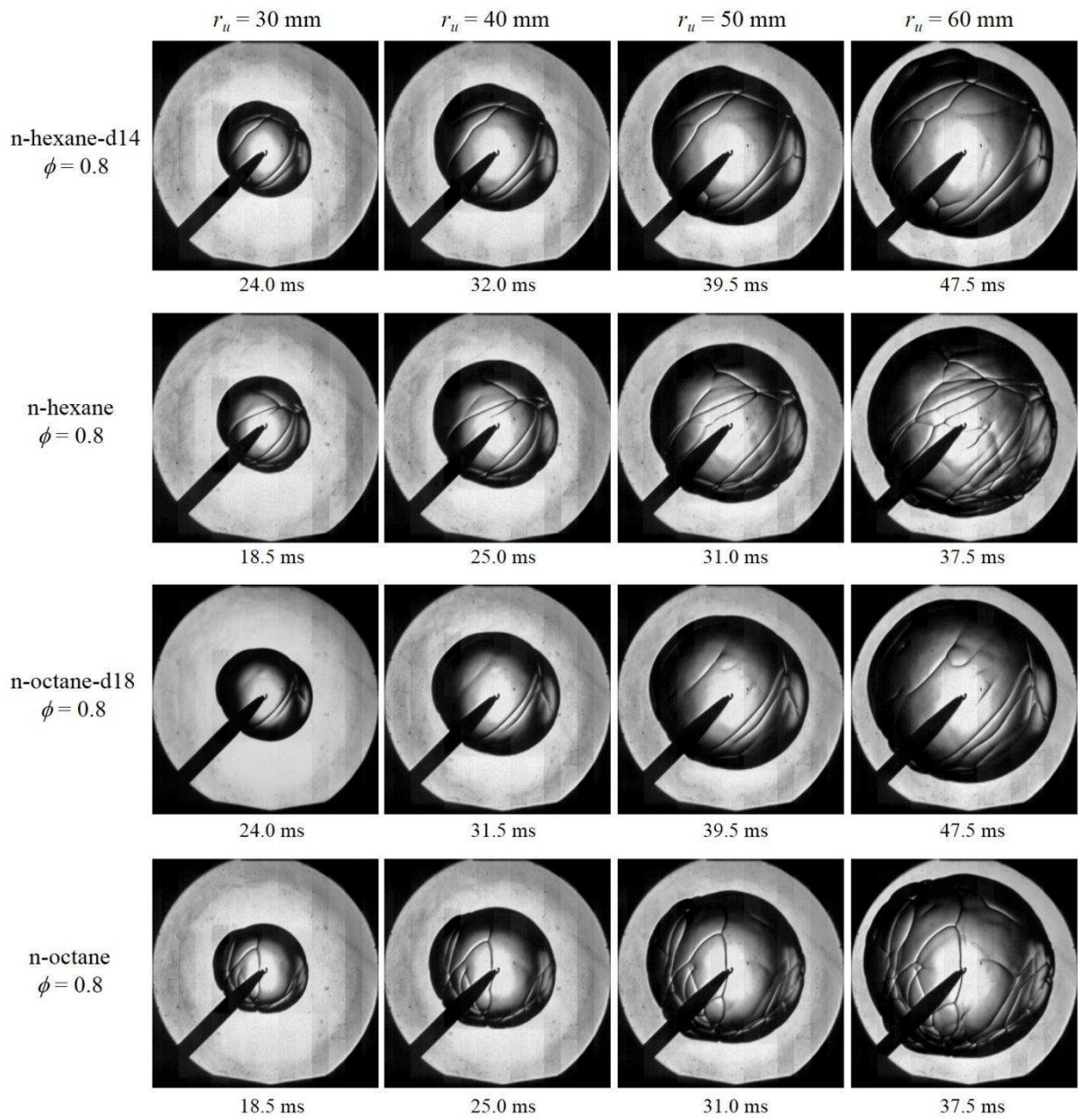
All schlieren based turbulent burn rates, u_{te} , refer to a mean flame radius of 30 mm. Reasons behind this choice are discussed in [6]. As a brief recapitulation here, presentation of the turbulent burn rate results at this radius offered the best compromise between ensuring that the flame had experienced most ($\sim 62\%$ [25]) of the effective turbulence [37] inside the vessel, while also avoiding extra difficulties during image processing induced due to flame convection from the centre of the visible area of the vessel, which is a particular problem for lean, high turbulence flames [24].

3.1 Laminar Burning Velocities of the Alkanes

The development of spherical expanding flames of normal and deuterated hexane and octane is depicted via the sequences of schlieren images displayed in Figure 1 for $\phi = 0.8$ and Figure 2 for $\phi = 1.0$. Starting at mean flame radii of 30 mm, the images of each of the flame filmstrips are in steps of 10 ± 0.2 mm in mean flame radius. Also shown below each image is the time elapsed from the first visible flame kernel following ignition. Although lean flames did not exhibit transition to fully cellular structure within the field of view of the bomb windows, the formation of large scale cells on the flame surface was more apparent for the normal than for the deuterated alkanes at radii of 60 ± 0.2 mm. Flames at stoichiometric conditions became fully cellular at ca. 45 mm for the normal alkanes and at ca. 50 mm for the deuterated alkanes. This is linked to differences in the thermo-diffusive properties at the flame front [35, 38], which in this case have been induced solely by the isotope effect. Note that the definition of the onset of cellularity was based on photographic observations for the formation of small scale cells at the flame surface

178 (Figures 1 and 2) in conjunction with identification of the point at which an appreciable flame
 179 acceleration appears on the plot of burning velocity vs. mean flame radius, as described in [7,
 180 35].

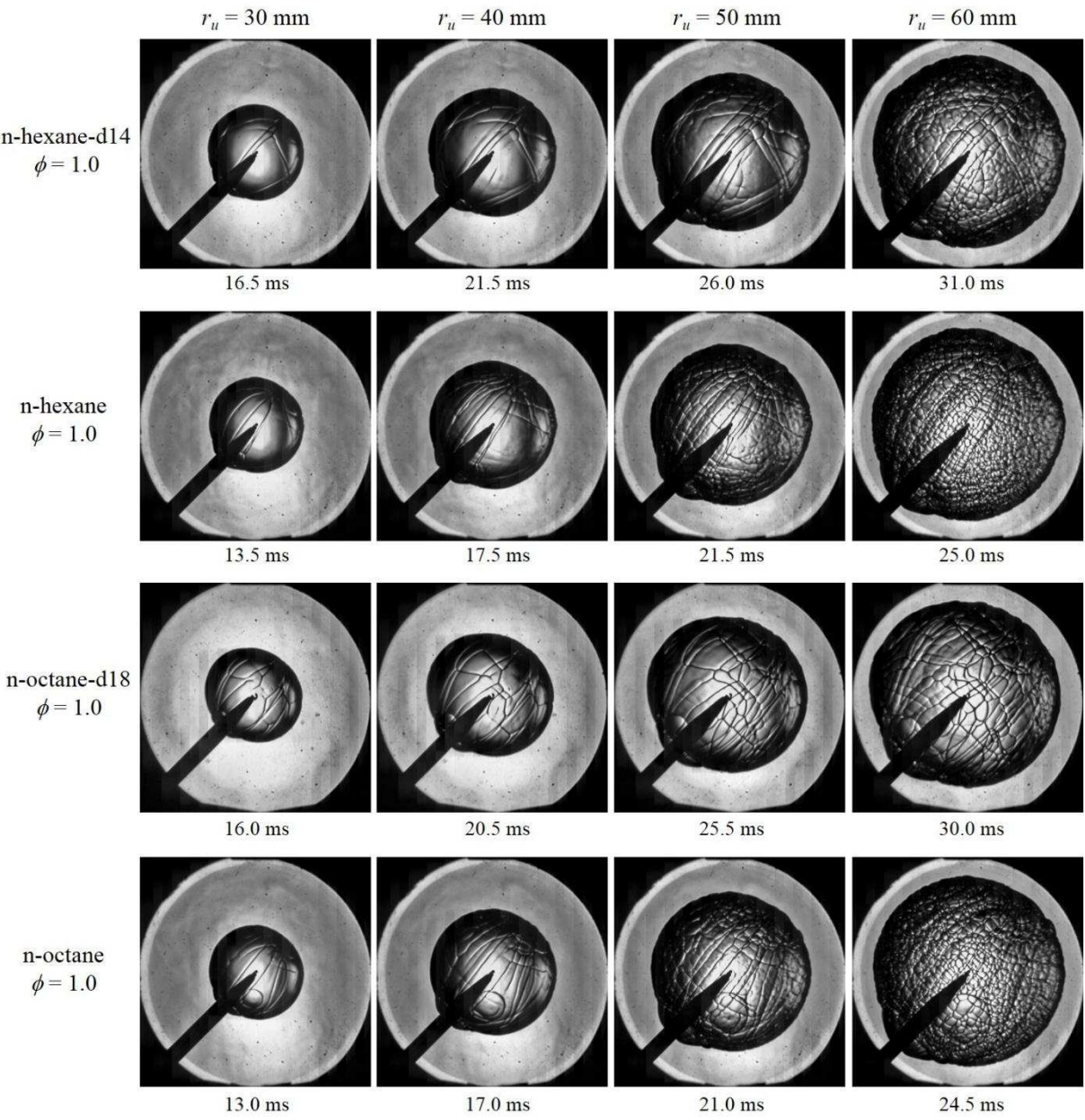
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182

183 Figure 1 – Filmstrip (left to right) of schlieren images showing the flame development for normal
 184 and deuterated alkane flames of $\phi = 0.8$. The mean flame radius values indicated have an
 185 accuracy of ± 0.2 mm, while the time values shown in milliseconds represent time elapsed from
 186 the first visible flame kernel following ignition.

187



188

Figure 2 – Filmstrip (left to right) of schlieren images showing the flame development for normal and deuterated alkane flames of $\phi = 1.0$. The mean flame radius values indicated have an accuracy of ± 0.2 mm, while the time values shown in milliseconds represent time elapsed from the first visible flame kernel following ignition.

The onset of apparent transition to fully cellular flames is specified on the u_n vs r_u plots of Figure 3 via the red asterisk symbols on top of the data points. Also specified on these plots is the early flame development region affected by the characteristics of the igniter. Spark energy much above the minimum ignition energy, can cause a very high initial flame speed due to the expansion of the plasma and the conductive energy transfer from it; these data are disregarded [26]. Previous measurements in the same apparatus have shown the spark affected area to be up to a mean flame radius of 8-10 mm [36]. For lean flames the slight increase in burning velocity with radius is attributed to the reduction of stretch rate with flame radius, as well as to a small increase of ~ 10 K in unburned gas temperature over that period of flame development [24]. Stoichiometric flames exhibited similar behaviour up to the point of transition to fully cellular regime, upon which a slight increase in flame acceleration was observed, for reasons described in [7]. For completion, the variation of burning velocity with stretch rate (α) is shown in Figure 4, along with the range of data over which the laminar flame theory described in [26] was applied to determine the true laminar, one-dimensional and unstretched burning velocities, u_l .

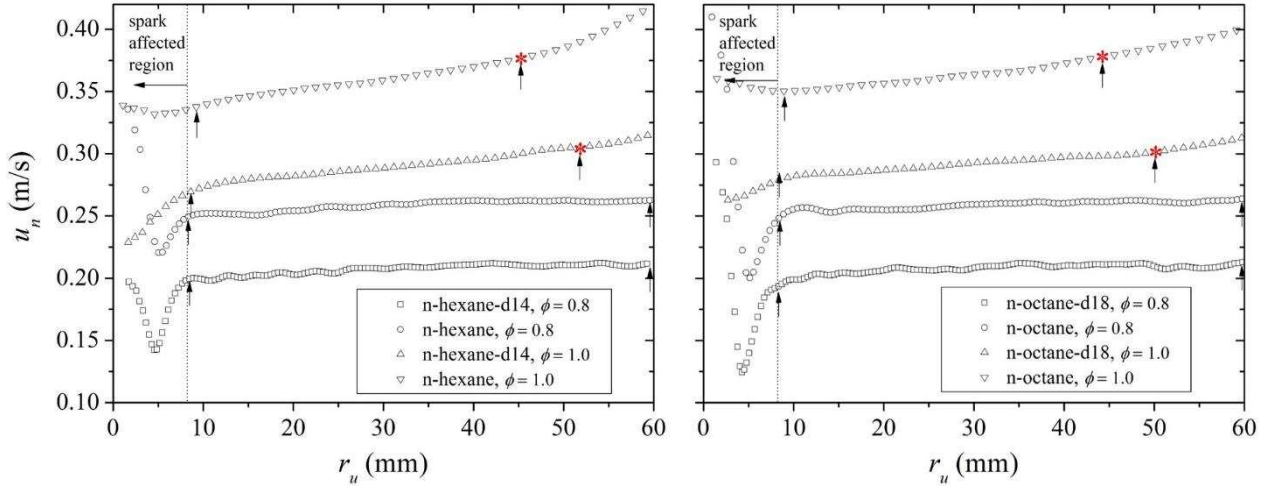


Figure 3 – Stretched burning velocity, u_n , plotted against mean flame radius, r_u , for normal and deuterated alkanes at $\phi = 0.8$ and 1.0. Vertical arrows indicate the data regions used for application of laminar burn rate theory to obtain unstretched burning velocity and Markstein lengths. The red asterisks indicate the onset of transition to fully cellular regime.

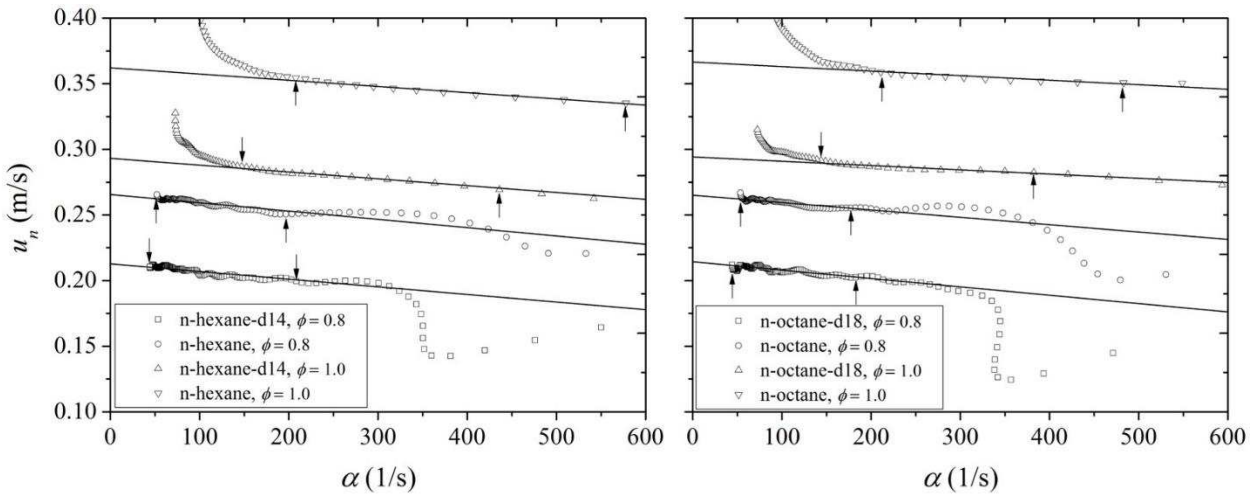


Figure 4 – Variation of stretched burning velocity, u_n , with stretch rate, α , for the normal and deuterated alkanes at $\phi = 0.8$ and 1.0. Vertical arrows indicate the data regions used for application of laminar burn rate theory to obtain unstretched burning velocity and Markstein lengths

Data for u_l , $u_{n,10mm}$ and $u_{n,30mm}$ are presented in tabulated form in Tables 1 for $\phi = 0.8$ and Table 2 for $\phi = 1.0$. The deuterated alkanes were found to burn approximately 20% slower than their normal alkane counterparts, a proportion that was independent of equivalence ratio, flame radius or whether the flame was unstretched or stretched.

	n-C ₆ H ₁₄ (m/s)	n-C ₆ D ₁₄ (m/s)	$u_{C_6D_{14}} / u_{C_6H_{14}}$	n-C ₈ H ₁₈ (m/s)	n-C ₈ D ₁₈ (m/s)	$u_{C_8D_{18}} / u_{C_8H_{18}}$
u_l	0.266 ± 0.001	0.214 ± 0.002	0.805	0.265 ± 0.001	0.214 ± 0.001	0.808
$u_{n,10mm}$	0.253 ± 0.002	0.202 ± 0.005	0.798	0.251 ± 0.007	0.198 ± 0.001	0.789
$u_{n,30mm}$	0.260 ± 0.001	0.212 ± 0.006	0.814	0.258 ± 0.002	0.208 ± 0.001	0.806

Table 1 – Measured average laminar burning velocities for normal and deuterated alkanes at $\phi = 0.8$, with $T_i = 360$ K and $P_i = 0.5$ MPa. Also included are the standard deviation of the measured values and the ratios of the measured burn rates of deuterated over normal alkanes.

	n-C ₆ H ₁₄ (m/s)	n-C ₆ D ₁₄ (m/s)	$u_{C_6D_{14}} / u_{C_6H_{14}}$	n-C ₈ H ₁₈ (m/s)	n-C ₈ D ₁₈ (m/s)	$u_{C_8D_{18}} / u_{C_8H_{18}}$
u_l	0.366 ± 0.005	0.292 ± 0.003	0.798	0.364 ± 0.003	0.294 ± 0.004	0.807
$u_{n,10mm}$	0.343 ± 0.005	0.274 ± 0.002	0.799	0.346 ± 0.005	0.281 ± 0.001	0.812
$u_{n,30mm}$	0.361 ± 0.001	0.288 ± 0.003	0.798	0.362 ± 0.003	0.293 ± 0.002	0.809

Table 2 – Measured average laminar burning velocities for normal and deuterated alkanes at $\phi = 1.0$, with $T_i = 360$ K and $P_i = 0.5$ MPa. Also included are the standard deviation of the measured values and the ratios of the measured burn rates of deuterated over normal alkanes.

The burned gas Markstein length, L_b , is a physico-chemical flame parameter used to characterise the effect of stretch rate on burn rate [35]. A small value of L_b is indicative of small influence of

237 flame stretch rate on burning velocity [26]. Burned gas Markstein lengths were determined as the
 238 slope of the linear fits in the u_n vs α plots (Figure 4). It should be noted that compared to the
 239 linear stretch corrections employed here, application of non-linear stretch corrections for the
 240 same data led to differences smaller than the experimental accuracy. Average L_b results for the
 241 conditions explored here are shown in Table 3 and demonstrate great similarity between the
 242 normal and deuterated alkanes, hence supporting the interpretation that the difference in burning
 243 velocity was independent of flame stretch (i.e. as shown in Tables 1 and 2). The similarity in L_b
 244 between the alkanes examined is likely to be due to their similar molar masses.

245

	n-C ₆ H ₁₂ , L _b (mm)	n-C ₆ D ₁₂ , L _b (mm)	n-C ₈ H ₁₆ , L _b (mm)	n-C ₈ D ₁₆ , L _b (mm)
$\phi = 0.8$	0.37 ± 0.020	0.37 ± 0.019	0.38 ± 0.049	0.39 ± 0.009
$\phi = 1.0$	0.33 ± 0.004	0.32 ± 0.012	0.27 ± 0.025	0.23 ± 0.044

246

247 Table 3 – Measured average Markstein lengths, L_b , for the normal and deuterated alkanes. Also
 248 included is the standard deviation between measurements performed at given equivalence ratios.

249

250 Normal versus deuterated alkanes have no differences in molecular structure and equilibrium
 251 calculations revealed negligible differences in adiabatic flame temperature, T_{ad} . Likewise,
 252 computations suggested very similar thermal and mass diffusion coefficients for these fuel-air
 253 mixtures (Table 4). The estimates displayed in Table 4 were based on the kinetic theory of gases
 254 developed by Chapman and Enskog and described in detail in [39], in conjunction with multi-
 255 component transport coefficients derived with the use of the equations defined in [40]. The
 256 thermodynamic data required for the calculations were provided by ExxonMobil [41]. Collision
 257 radii and reduced energies for the application of the kinetic theory of gases were estimated from

critical temperature and pressure data found in the NIST online library [42]. It may thus be concluded that since the values of thermal and mass diffusivity of the deuterated and normal alkane-air mixtures are virtually identical, the observed difference in burning velocities cannot be attributed to transport properties of the fuel molecule.

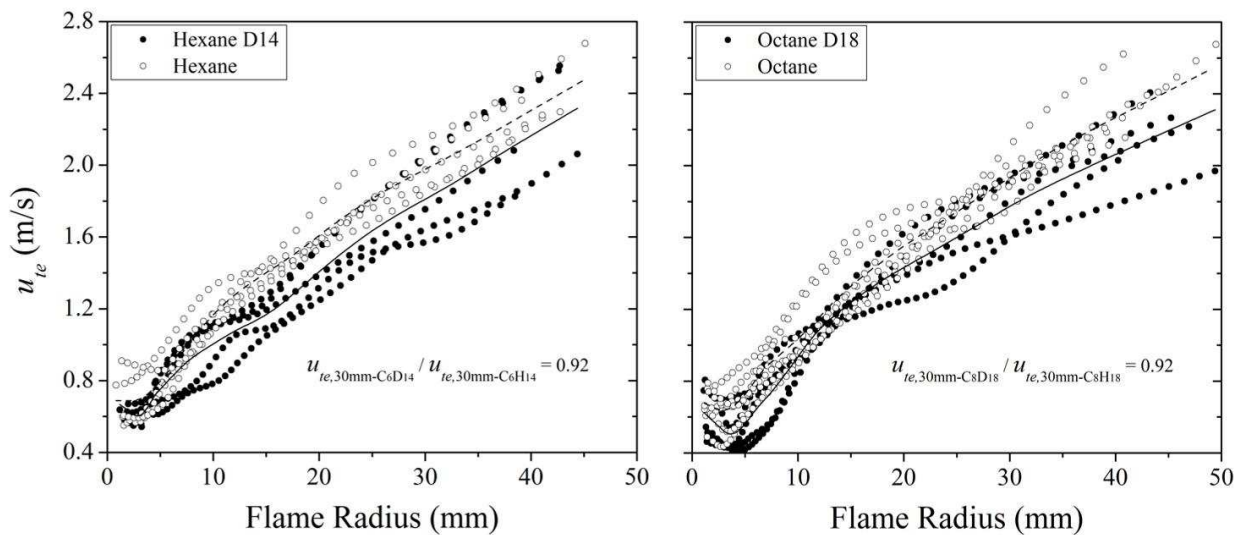
Temperature, T	$\frac{a_{\text{C}_6\text{D}_{14}\text{-air}}}{a_{\text{C}_6\text{H}_{14}\text{-air}}}$	$\frac{a_{\text{C}_8\text{D}_{18}\text{-air}}}{a_{\text{C}_8\text{H}_{18}\text{-air}}}$	$\frac{D_{\text{C}_6\text{D}_{14}\text{-air}}}{D_{\text{C}_6\text{H}_{14}\text{-air}}}$	$\frac{D_{\text{C}_8\text{D}_{18}\text{-air}}}{D_{\text{C}_8\text{H}_{18}\text{-air}}}$
360 K	0.995	0.997	0.973	0.977
$T = T_{\text{ad}} \approx 2350 \text{ K}$	1.000	0.999	0.974	0.978

Table 4 – Ratios of thermal, α , and mass, D, diffusivities of deuterated versus normal alkane-air stoichiometric mixtures at 360 K and $T = T_{\text{ad}}$, at constant pressure of 0.5 MPa.

To put the reduction of the laminar burning velocity of the deuterated alkanes relative to their respective hydrogen-containing counterparts in perspective, it was recently shown [6] that for identical conditions (T_i , P_i , ϕ), the unstretched burning velocity of the hexane isomer, 2,2-dimethyl butane, was measured to be 15% lower than that of n-hexane. This difference may be attributed to (i) the potential for the production of a higher proportion of CH_3 radicals during branched alkane combustion relative to those generated during n-alkane combustion, and (ii) the predominance of primary C-H bonds relative to the number of secondary C-H bonds in the n-alkane [4, 6]. Any causes of the 20% difference measured here between n-hexane and n-hexane-d14 pertaining to chemistry are limited to kinetic isotope effects of reaction rates involving H versus D atoms derived from the primary fuel molecule or contained in other combustion intermediates. However, a very important, supplementary factor which also affects laminar flame propagation is the lower diffusivity of D versus H atoms.

3.2 Turbulent Burning Velocities of the Alkanes

280 Turbulent tests were performed solely at $\phi = 1.0$ for a turbulent r.m.s. velocity of 4 m/s. Schlieren
 281 derived turbulent burn rates plotted against flame radius are shown in Figure 5. The reasoning
 282 behind setting 30 mm as the reference mean flame radius was explained at the beginning of
 283 Section 3. It was found that the deuterated fuels remained slower than their conventional
 284 counterparts under turbulence. However, the differences were substantially reduced compared to
 285 the laminar flames. Nevertheless, overall reductions throughout flame development subsequent to
 286 the spark affected region remained at 5-10% as a result of the substitution of H for D in both of
 287 the alkanes that were studied here. The average difference in burn rate between normal and
 288 deuterated alkanes at the reference radius of 30 mm was 8% (Figure 5).



289
 290 Figure 5 – Turbulent burning velocities ($u' = 4$ m/s) for the alkanes plotted against mean flame
 291 radius. The curves in the plots are averages at set radii obtained via linear interpolation; dashed
 292 lines for normal alkanes, solid lines for deuterated alkanes. Also shown are ratios of the normal
 293 vs. deuterated alkane at the reference radius of 30 mm.

294
 295 A similar reduction of the differences between the burn rates of various hydrocarbon fuels when
 296 moving from laminar to turbulent conditions was reported in the previous paper [6] of the overall

study, which addressed the influence of molecular structure for a series of C₆ hydrocarbon fuels. As discussed in Section 3.1, the unstretched laminar burning velocity of 2,2 dimethyl butane has been found to be ~15% lower than that of n-hexane for near stoichiometric conditions, at 0.5 MPa and 360 K [6]. However, at the same equivalence ratio, pressure and temperature, the turbulent burning velocity of 2,2 dimethyl butane was only ~9% lower than that of n-hexane (at $u' = 2$ m/s and 6 m/s). Similarly [6], at the same equivalence ratio, pressure and temperature conditions, 2-methyl pentane was measured to have ~11% lower laminar burn rate than n-hexane, whereas its turbulent burn rate was found to be ~5% slower than that of n-hexane at $u' = 2$ m/s and 6 m/s. These observations indicate that there are residual kinetic and transport processes influencing turbulent combustion. In the case of the C₆ work reported in [6], the kinetic differences were primarily linked to the propensity of production of CH₃ vs C₂H₅ radicals during the initial steps of fuel oxidation and, consequently, the availability of H radicals and the facilitation of branching reactions at the flame front. Likewise, in the current work, the relative differences between the turbulent burn rate of the normal and deuterated alkanes studied here point to a specific contribution to turbulent flame propagation of the kinetics and transport processes involving H and D atoms and related radicals, such as OH / OD or HO₂ / DO₂.

Based on the turbulent regime theory [43], the alkane flames explored were classified as thickened flamelets, for which the Kolmogorov turbulent scale, η , is typically less than the laminar flame thickness, δ_l , and hence turbulence can penetrate the flame and alter the transport and chemistry of species at the flame front. In this case, application of the Zimont submodel for turbulent burning velocity [44], which has been extensively discussed elsewhere [45], is valid.

$$u_{te} \sim u^{0.75} L^{0.25} u_l^{0.5} \alpha^{-0.25} \quad (1)$$

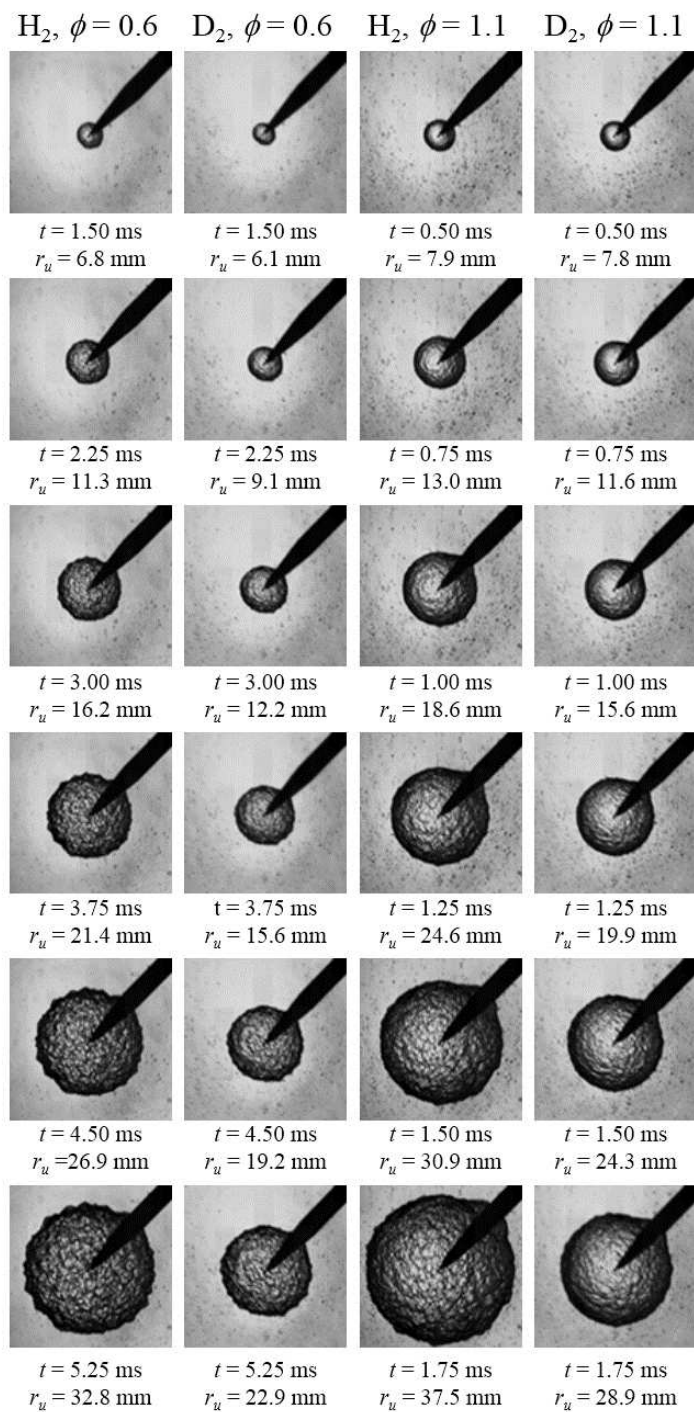
In this work, u' , the rms turbulent velocity, and L , the integral length scale of turbulence, remained constant for all flames. The reduced differences measured when moving from laminar to turbulent conditions were adequately replicated via application of Eq. (1). Utilising u_l and α data from Tables 2 and 4, it can be shown that the turbulent burn rate ratios of C_6D_{14} / C_6H_{14} and C_8D_{18} / C_8H_{18} predicted via Eq. (1) are 0.898 and 0.899, i.e. very similar to those experimentally measured at 0.9 – 0.95 throughout flame development within the vicinity of the bomb windows. Application of Eq. (1) for the C_6 hydrocarbon pairs can be shown to yield similarly good agreement between predictions and actual measurements. Therefore, it could be concluded that for fuels of similar molar mass, and consequently transport properties, the kinetic processes at the flame front only influence turbulent burning velocity indirectly, through the laminar burning velocity accordingly to Eq. (1).

3.3 Laminar Burning Velocities of H_2 and D_2

The development of the leanest and richest hydrogen-air and deuterium-air flames examined in the current study is illustrated via the filmstrips of schlieren images shown in Figure 6. These images have been zoomed in to better demonstrate the extremely early transition to cellular regime almost immediately following ignition (i.e. at $r_u < 10$ mm) for both fuels. To demonstrate the laminar flame development, shown in Figure 7 are plots of stretched laminar flame speed, u_n , versus flame radius for the leanest and richest deuterium and hydrogen flames examined.

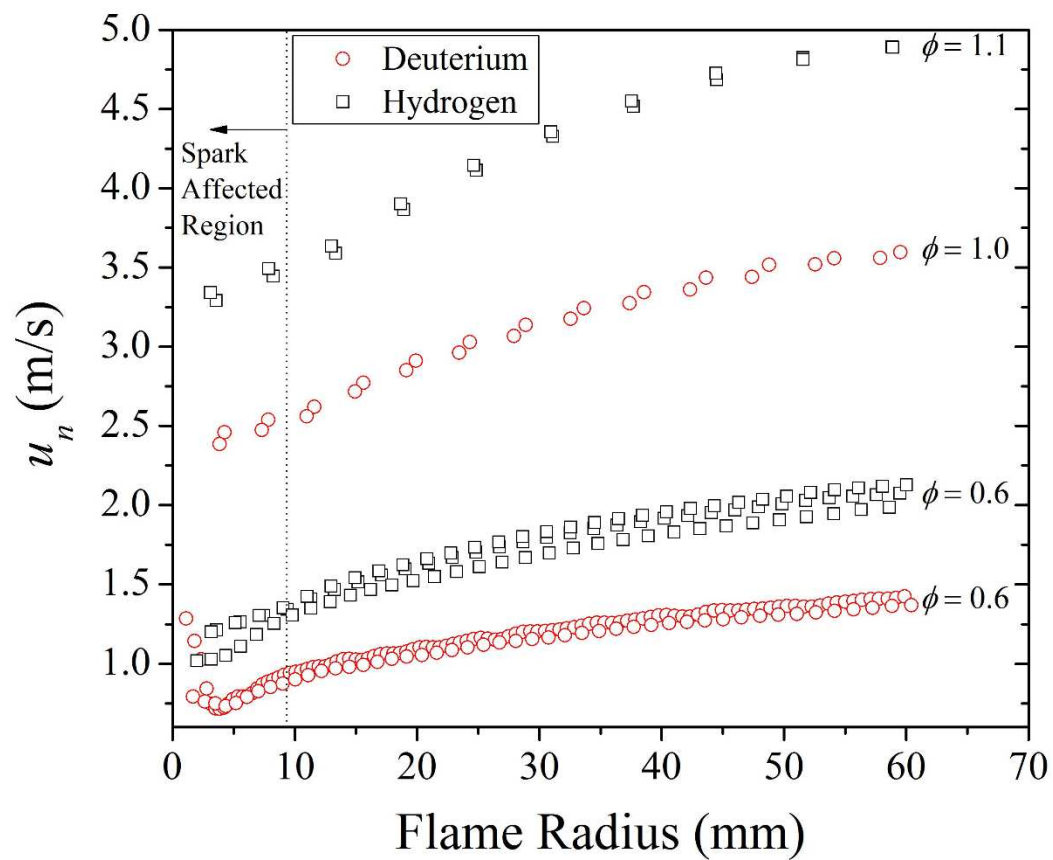
The results for the stretched laminar burning velocities, u_n , at mean flame radii of $r_u = 10$ mm and 30 mm are displayed in Figure 8. It is important to clarify that these burning velocities do not reflect the pure, one-dimensional, unstretched laminar burning velocity (u_l). The reason is the extremely early transition of the H_2 and D_2 flames to a cellular regime, which made application of

342 the laminar flame theory to calculate u_l impossible [26]. Hence, in the case of the results of
343 Figure 8, diffusion effects are twofold, as they also include the increased diffusivity arising from
344 the increased surface area induced by cellularity. This effect is not expected to be identical
345 between H_2 and D_2 flames. The propensity to cellularity in fuel-air flames is believed to be
346 related to the Lewis number, $Le = \alpha_{mix} / D_{\text{deficient reactant}}$, of the deficient reactant [34].
347 Computations following the methods described in [39] and [40] showed that at $0.6 \leq \phi < 1.0$,
348 where fuel is the deficient reactant, Lewis numbers for H_2 -air flames were 20-25% smaller than
349 those for D_2 -air flames. Hence, instability effects are anticipated to be more prominent in H_2 than
350 in D_2 at $0.6 \leq \phi < 1.0$.



351

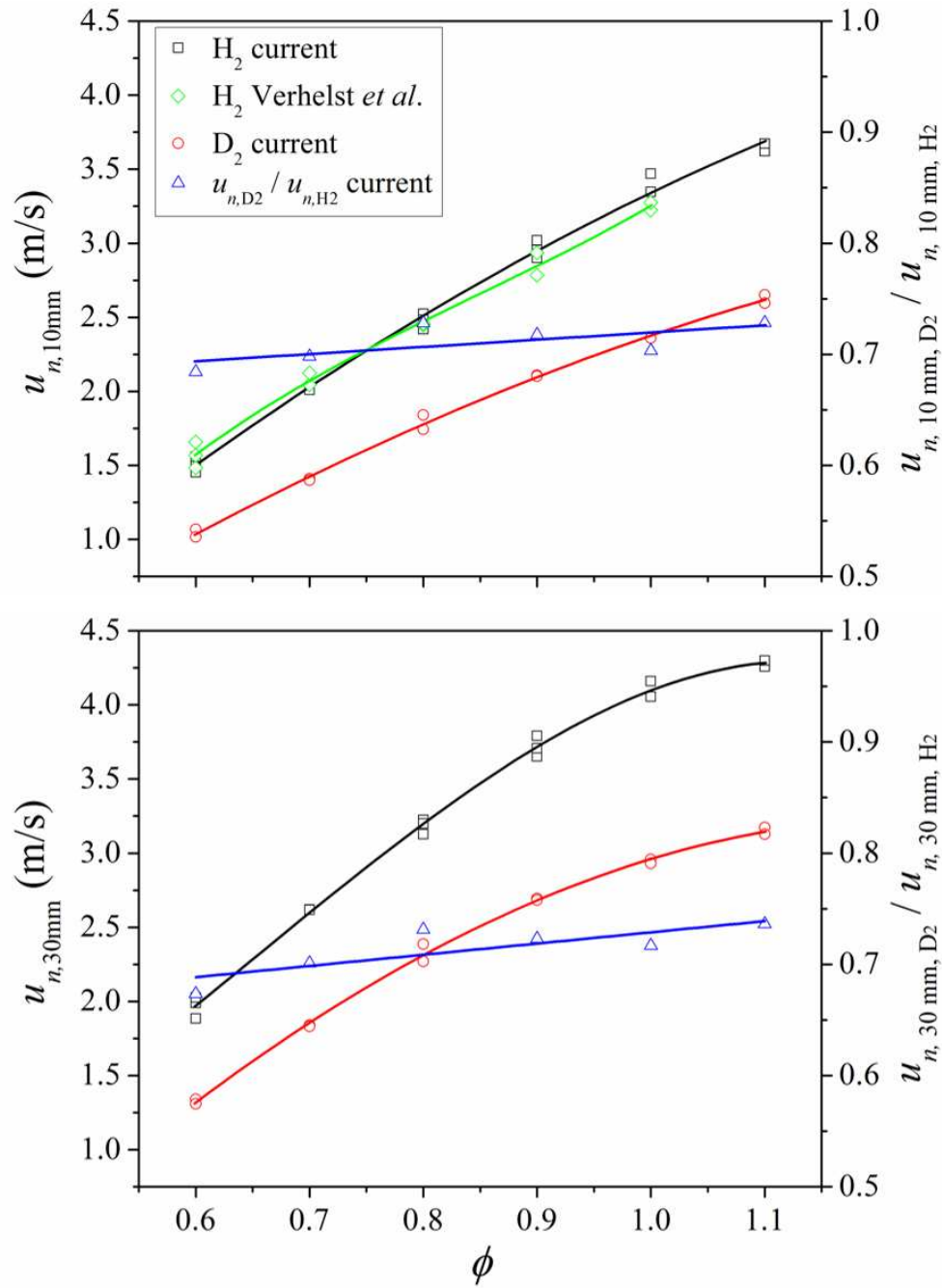
352 Figure 6 – Filmstrip (top to bottom) of schlieren images showing the flame development for
 353 hydrogen-air and deuterium-air flames at $\phi = 0.6$ and $\phi = 1.1$. The time values shown in ms
 354 represent time elapsed from the first visible flame kernel following ignition.



355

356 Figure 7 – Plots of stretched burning velocity versus flame radius showing the flame
 357 development of the leanest and richest hydrogen and deuterium flames studied.

358



359

360 Figure 8 – Schlieren based laminar burn rates for H_2 -air, D_2 -air flames at mean flame radii of 10
 361 mm and 30 mm, plotted versus ϕ . The curves are 3rd order polynomial fits of the experimental
 362 data. Also included in the plot for mean flame radius of 10 mm (top) are data for the burn rate of
 363 H_2 reported in [13] at identical conditions.

364

365 Focusing on the results of Figure 8, an increase in burn rate with ϕ was measured for both fuels
366 over the range of ϕ explored. The ratio $u_{n,D2} / u_{n,H2}$ varied from 0.69 ± 0.05 at $\phi = 0.6$ to $0.73 \pm$
367 0.1 at $\phi = 1.1$ for both flame radii assessed. These findings are almost identical to those reported
368 in [19] for hydrogen and deuterium flames with oxygen, albeit this earlier paper did not indicate
369 whether the flames were cellular.

370 Data reported in [13] for hydrogen-air mixtures are compared with the schlieren derived laminar
371 burn rates for H_2 -air reported here (Figure 8, top graph). The apparatus and initial conditions used
372 in the two studies were identical. Differences in the burn rates ranged from $\sim 1\%$ at $\phi = 0.6$ to a
373 maximum of $\sim 4\%$ at $\phi = 1.0$. These small discrepancies could be attributed to uncertainties in the
374 equivalence ratio and slight differences in the imaging equipment and processing technique used.
375 In another study of H_2 combustion performed in the Leeds MkII bomb [10], utilisation of a faster
376 digital camera system enabled the determination of unstretched laminar burning velocities.
377 Values of u_l reported in [10] were 30-40% lower compared to the $u_{n,10mm}$ values presented here,
378 with the percentage difference becoming smaller with increasing ϕ . Given that there is a very
379 early transition from laminar to cellular H_2 flames, and especially for lean flames, these
380 differences could be attributed, primarily, to the effect of cellularity and, secondarily, to the effect
381 of stretch rate.

382 To enable interpretation of the observed behaviour, computations for T_{ad} and transport
383 coefficients were performed using the methods cited in Section 3.1 for the alkanes. In this case,
384 any additional thermodynamic data required for the calculations was found in [46]. Although the
385 overall predicted trend in T_{ad} vs ϕ was consistent with that for the laminar burn rate vs ϕ (cf.
386 Figure 9a and Figure 8), the differences between the adiabatic flame temperature for H_2 and D_2 at
387 a given equivalence ratio were too small to account for the measured differences in their laminar

388 burn rates. Also included in Figure 9 are computations for the ratios of thermal diffusivity of the
 389 mixtures, $\alpha_{D_2\text{-air}} / \alpha_{H_2\text{-air}}$ (Fig. 9b), and effective mass diffusivities, D_{D_2} / D_{H_2} (Fig. 9c), and $D_D /$
 390 D_H (Fig. 9d), at the constant pressure (0.5 MPa) adiabatic flame temperature. Computed values
 391 for $\alpha_{D_2\text{-air}} / \alpha_{H_2\text{-air}}$ ranged between 0.81 at $\phi = 0.6$ and 0.75 at $\phi = 1.1$. Values for the mass
 392 diffusivities were calculated to be $D_{D_2} / D_{H_2} \sim 0.66$ and $D_D / D_H \sim 0.73$ at all equivalence ratios
 393 explored. The ratios for D_{D_2} / D_{H_2} given here are consistent with that derived by Gray et al [20],
 394 for which $D_{D_2} / D_{H_2} = 0.72$ over a range of burnt gas compositions of $H_2 - O_2$ and $D_2 - O_2$ flames
 395 at low pressure. Based on a dependence of flame speed proportional to \sqrt{D} , they attributed a
 396 maximum decrease in flame speed in deuterium-containing mixtures to be 0.85 of that in
 397 hydrogen-containing mixtures. This is insufficient to account solely for the overall differences
 398 observed in the burning velocities.

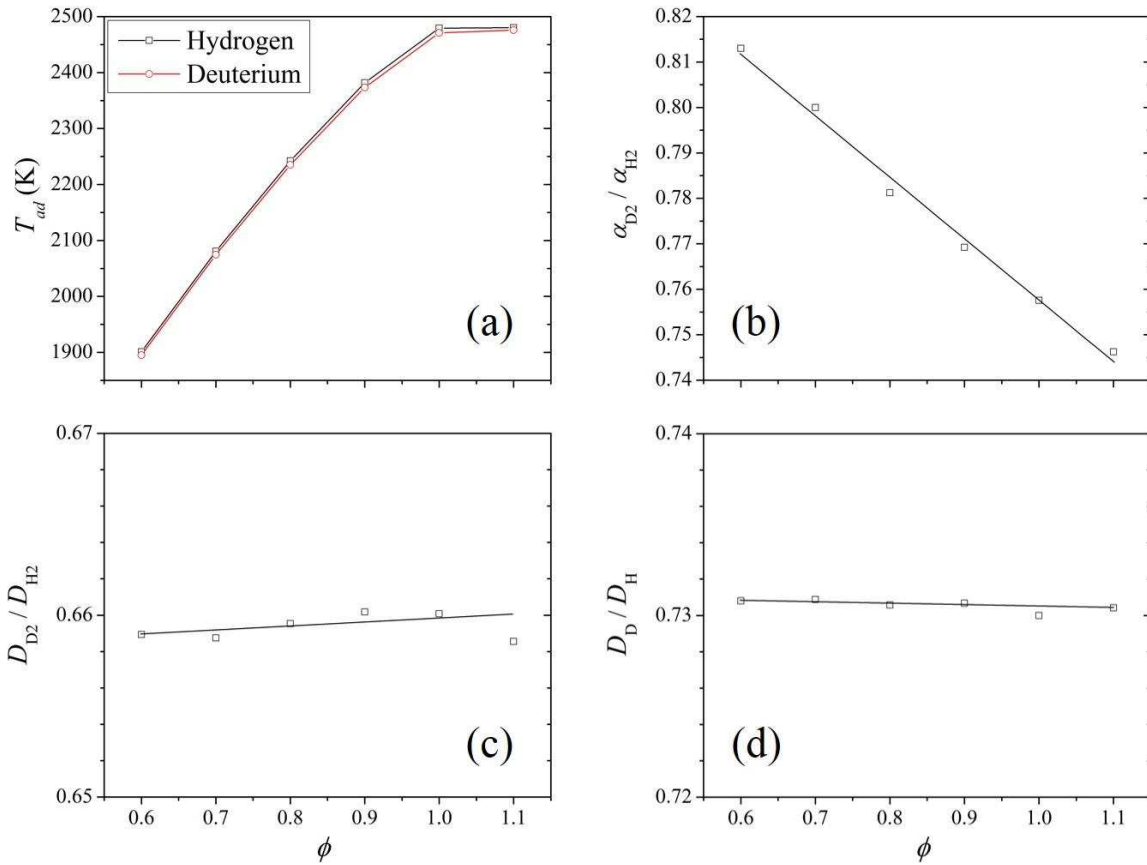


Figure 9 – Computed adiabatic temperatures for H₂-air, D₂-air flames for initial conditions of 360 K and 0.5 MPa. Also shown are ratios of thermal diffusivities of D₂ over H₂ and mass diffusivities of D₂ over H₂ and D over H calculated at the constant pressure (0.5 MPa) adiabatic flame temperature.

Numerous studies [e.g. 11, 47-48] have highlighted the critical importance of reactions R1 to R4 on controlling the burning velocity of H₂-air flames.



The burn rate of the D₂ – air system is similarly controlled by the equivalent reactions. However, their rates will be susceptible to kinetic isotope effects, which must effect the corresponding rate constants. The ratios, k_D/k_H , for the forward Reactions R1 – R4 are displayed in Figure 10. Data were taken from references [20, 49]. The computations showed that the rate constants of D₂ were approximately 0.71, 0.62, 0.8 and 0.5 times those of H₂ for reactions R1, R2, R3 and R4, respectively. An analysis by Gray et al [20] attributed a geometric mean of the ratio of the rate constants (k_D/k_H) for reactions R1 – R3 at 2500K to be 0.59.

The dependence of the laminar burning velocity on the fundamental physical and kinetic parameters has been described as $u_n \sim (\alpha \cdot \omega)^{0.5}$, where α is the thermal diffusivity of the mixture and ω is the global reaction rate [50]. This approximation is likely to be more valid for the relatively simple H₂-air and D₂-air combustion systems, than for those of hydrocarbon fuels. The laminar burn rate of deuterium could thus be estimated via,

423

$$u_{n,D2} \sim \left(\frac{(a.\omega)_{D2}}{(a.\omega)_{H2}} \right)^{0.5} \cdot u_{n,H2} \quad (2)$$

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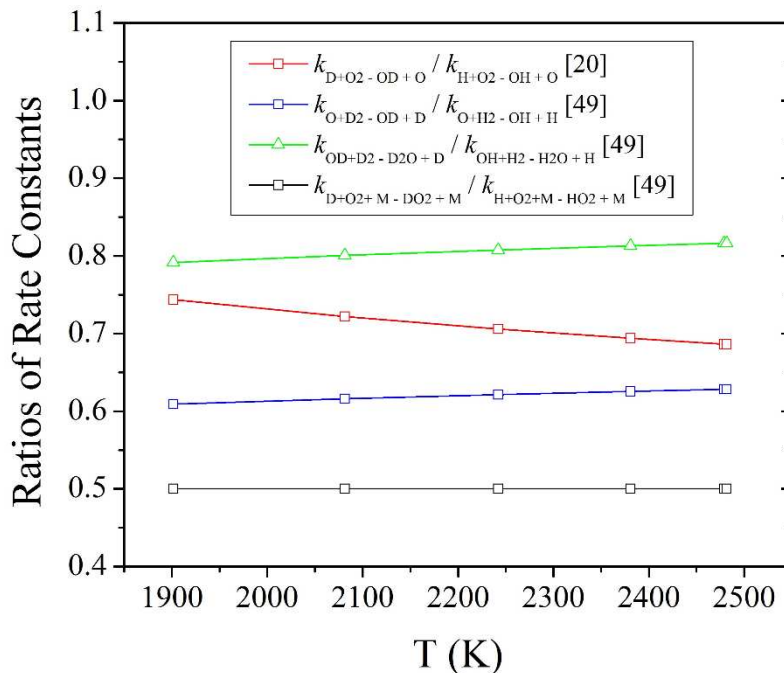
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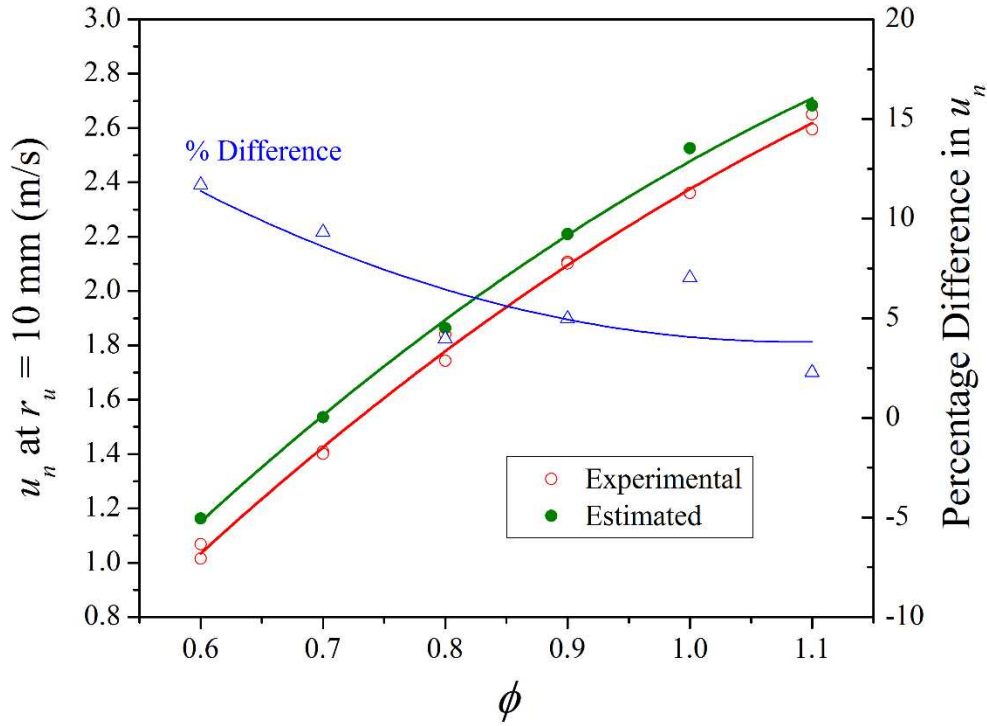
435

The reaction rate terms in Eq. (2) were set to be equal to the weighted average of the reaction rates of the critically important Reactions R1-R4. This weighted average was based on laminar burn rate sensitivity factors, S_i , reported in [11]. More specifically, to get the global reaction rate ratio of Eq. (2), the k_D/k_H ratios for reactions R1 – R4 (Figure 10) were multiplied by weighted laminar burn rate sensitivity factors, determined as $S_{i,w} = S_i / \sum S_i$. The values used for the thermal diffusivity ratio of equation 2 were those displayed in Figure 9b. The $u_{n,D2}$ values estimated via equation 2, combined with experimental $u_{n,H2}$ data, are shown in Figure 11. Agreement with the experimentally measured laminar burn rates of D_2 -air flames is good. The difference ranged from ca. 12% at $\phi = 0.6$ to ca. 2% at $\phi = 1.1$. The over-prediction at lean mixtures could be attributed to the effects of cellularity, encapsulated in the experimentally determined $u_{n,H2}$ data used for the estimate. The reasoning behind this was described at the beginning of this section, with respect to the discussion of the results of Figure 8.



436

437 Figure 10 – Ratios of selected reaction rate constants, k_{D2} / k_{H2} , at temperatures relating to the T_{ad}
 438 at each of the equivalence ratios for which burn rates were experimentally measured.

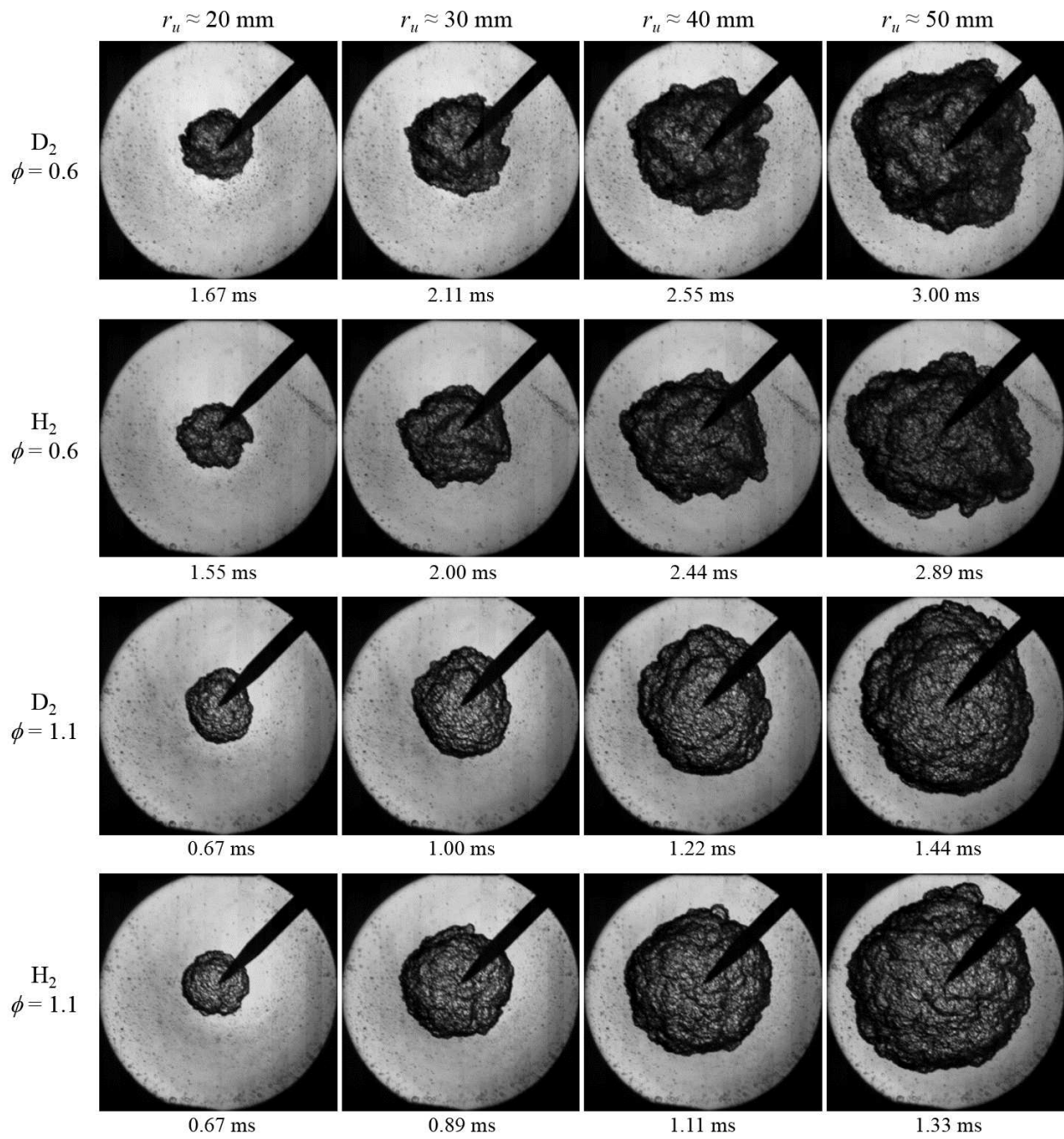


439
 440 Figure 11 – Comparison between measured and estimated burn rates of D_2 -air laminar flames at
 441 various equivalence ratios. The curves are 2nd order polynomial fits of the data, added for better
 442 illustration.

443 444 3.4 Turbulent Burning Velocities of H_2 and D_2 flames in air

445 For completeness, a filmstrip showing H_2 -air and D_2 -air flame images for the leanest and richest
 446 conditions explored in this study is included in Figure 12. For both fuels, lean flames appeared
 447 more distorted compared to rich flames. Schlieren derived turbulent burning velocities for H_2 and
 448 D_2 at mean flame radii of 30 mm and $u' = 4$ m/s, over the range $\phi = 0.6$ to $\phi = 1.1$, are displayed
 449 in Figure 13. To indicate the experimental scatter, also included in Figure 13 is the standard
 450 deviation from the average u_{te} values at each condition. The change from laminar to turbulent

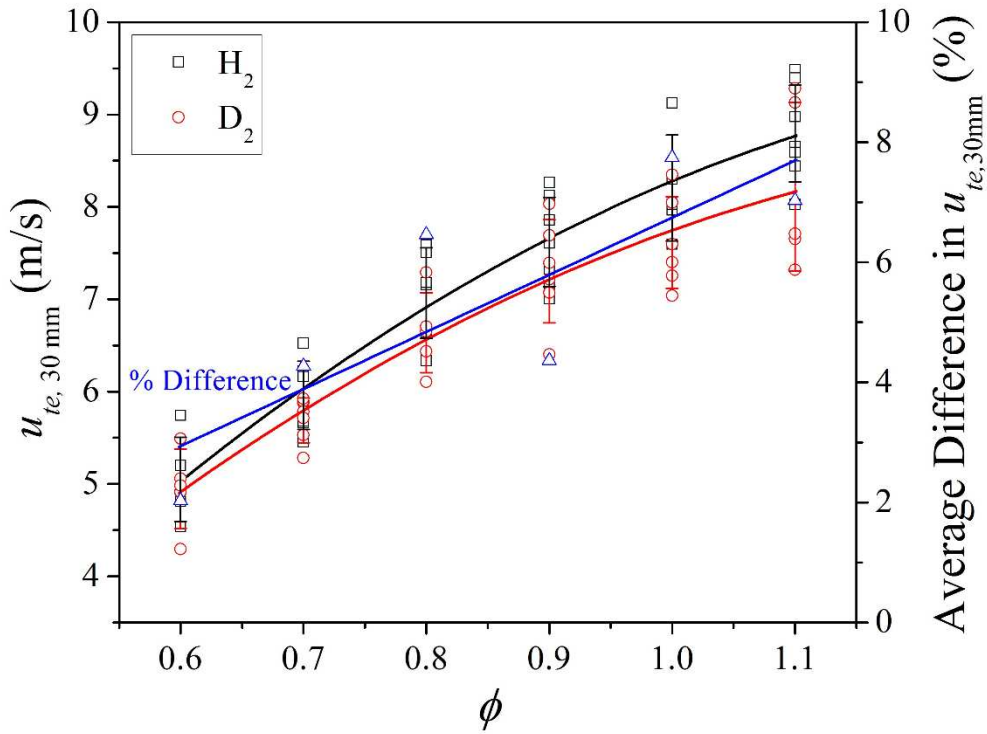
451 conditions resulted in a significant reduction in the burn rate differences between H_2 and D_2 .
 452 These differences fell from 25-30% under laminar conditions to $\sim 5\%$ when turbulence was
 453 present. This reduction was more marked than that for the normal vs deuterated alkanes, as
 454 discussed in Section 3.2.



456 Figure 12 – Filmstrips of turbulent flame images for H₂ and D₂ at equivalence ratios of 0.6 and
 457 1.1. The mean flame radius values indicated have minimum accuracy of ± 1.0 mm.

458

459 Although a general trend to lower turbulent burning velocities of D₂ flames relative to those of H₂
 460 is evident in Figure 12, the individual results tend to overlap within the range of experimental
 461 scatter. The similarity between the turbulent burning velocities of deuterium and hydrogen
 462 flames, contrasted with the marked difference of their laminar burning velocities, suggests that
 463 turbulent transport processes have a greater influence on the flame propagation rate than kinetic
 464 isotope effects involved in the kinetic chain branching reactions.



465

466 Figure 13 – Schlieren based turbulent burning velocities ($u' = 4$ m/s) for hydrogen and deuterium
 467 at a mean flame radius of 30 mm. The standard deviation from average experimental data at each
 468 condition along with the average percentage difference between the two fuels are also shown.

469

Application of Eq. (1) for the H₂ and D₂ flames examined is not as straightforward as for the normal and deuterated alkanes. First, for reasons discussed earlier in Section 3.3, the analysis for the H₂ and D₂ laminar flames could not yield a true unstretched laminar burning velocity, as required for appropriate application of Eq. (1). Second, owing to their very high laminar burn rate and small flame thickness, the H₂ and D₂ turbulent flames examined are classified as corrugated flames, in which case the condition of $\eta \ll \delta_l$ does not necessarily stand. Nonetheless, estimations made through Eq. (1) still are in fair agreement with the experiments. Estimations from Eq. (1) for the u_{te} ratio between D₂ and H₂ ranged from 0.88 at lean conditions to 0.94 at rich conditions.

4. Conclusions

Substitution of the hydrogen atoms in n-hexane and n-octane with deuterium atoms resulted in a reduction of ca. 20% in the measured laminar burning velocity, despite there being little difference in molar mass or calculated adiabatic flame temperatures, and no expectation of qualitative differences in the kinetic scheme for full oxidation of the normal and deuterated alkane counterparts. Also, it was assumed that the kinetic scheme for full oxidation of the normal and deuterated alkane counterparts were the same. The normal alkane flames were observed to become cellular slightly earlier. Nonetheless, insofar that comparisons were made with respect to the unstretched burning velocities calculated using data corresponding to the pre-cellular region of the flame, instability effects cannot be considered to be significant. It is concluded that the observed difference in laminar burn rates between normal and deuterated n-hexane and n-octane are the result, predominantly, of the higher thermo-diffusivity and reactivity of hydrogen atoms relative to those of deuterium atoms.

493 Measured laminar burn rates for H₂-air flames were 30% higher than for D₂-air flames, at fixed
494 ambient temperature, pressure and equivalence ratios. This difference was also linked to the
495 thermo-diffusive and chemical kinetic properties of H vs D atoms. The ratios of thermal and mass
496 diffusivity of deuterium over hydrogen atoms, as well as corresponding reaction rate ratios for the
497 important chain branching reactions involving D and H, were estimated to be within 0.6 – 0.8
498 over the range of conditions explored, which is very similar to the measured difference in laminar
499 burn rate. The higher laminar burn rate difference between H₂ and D₂ compared with that
500 measured for normal versus deuterated alkanes would be expected, in view of the kinetic
501 complexity and weakened isotope effect in the hydrocarbon combustion chemistry.

502 Under turbulent conditions, differences in the burn rate between normal and deuterated n-hexane
503 and n-octane were much smaller, with the deuterated alkanes being ~8% slower than their normal
504 counterparts. It is concluded that turbulence globally accelerates species diffusivity, rendering
505 transport properties of species within the preheat zone more important for turbulent compared to
506 laminar flames. Given that the thermal diffusivity of the parent fuels is almost identical between
507 the normal and deuterated alkane counterparts, the residual influence of kinetic isotope effects is
508 expressed as $u_l^{0.5}$.

509 The difference between the burn rates of H₂-air flames and D₂-air flames under turbulence was
510 reduced by a factor of five relative to that observed under laminar conditions. These findings
511 emphasise that transport properties, globally boosted by turbulent diffusivity, exert greater
512 control than kinetic isotope effects during turbulent combustion. The measured turbulent burning
513 velocity ratios at each mixture stoichiometry examined were adequately replicated via application
514 of the Zimont submodel for turbulent burning velocity, defined in Eq. (1).

515

Acknowledgements

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